

Problem Set 4

Quantum Harmonic Oscillator

1. For quantum harmonic oscillator with $\hbar\omega = 1$ calculate energy of transition:

a) $\Delta E_{3 \rightarrow 4}$ between levels $n=3$ and $n=4$. b) $\Delta E_{4 \rightarrow 5}$ between levels $n=4$ and $n=5$.

2. Calculate angular frequency for the oscillator with force constant $k=320$ N/m and mass $m=4 \times 10^{-18}$ kg.

3. Proof that $\hbar\omega = h\nu$, where $\hbar = h/2\pi$, ω - angular frequency (rad/sec) and ν - frequency in (sec^{-1})

4. Calculate the frequency in sec^{-1} which corresponds to the wavenumber $\frac{1}{\lambda} = 200 \text{ cm}^{-1}$

Hint: $\nu = \frac{c}{\lambda}$, where ν is the frequency, $c=3 \times 10^8$ m/s is speed of light, λ is the wavelength

5. Calculate Hermite polynomials a) $H_1(y)$; b) $H_2(y)$; c) $H_3(y)$